Problem 2: #FireGeno (30 points)

As of April 2016, the margin of victory per game by the UConn women's basketball team has a mean of 40 and a standard deviation of 10. Suppose the margin of victory per game follows a <u>normal</u> distribution.

(a) Using the Z-table, find the probability p (to 4 decimal places) that in a given game, UConn does NOT win by more than 20 points.

A shadow organization is unhappy with the fact that UConn does not always win by more than 20 points in every game. It issues the following #FireGeno decree, which proclaims that

"If, by the end of a <u>36-game season</u>, UConn fails to win by more than 20 points for a total of <u>3 games or more</u>, then Geno should be fired."

In what follows, you may assume that the point distribution in each game is independent and identically distributed. Express your answers in terms of p defined in Part (a).

- (b) What is the probability that the proclamation becomes true?
- (c) What is the probability that the proclamation becomes true on the 36th game?