Problem 6: UConn men's basketball vs. Ivy League opponents

Since the 1980-81 season, UConn men's basketball team has played 31 games against Ivy League opponents. And it has lost only twice: on Dec. 2, 1986 and on Dec. 5, 2014, both to Yale. For some perspectives, here are the relevant stats in a typical matchup:

| Random variable | Stands for | Mean | St. Dev. |
|-----------------|---|------|----------|
| X | Points scored by UConn per game | 75 | 15 |
| Y | Points scored by Ivy League opponent per game | 57 | 12 |

Also X and Y are not independent: the correlation between X and Y is $\frac{5}{8}$. Based on this information:

(a) Show, via an explicit computation, that the standard deviation of X - Y is 12. [Useful: $12^2 = 144$, $15^2 = 225$.]

(b) By the central limit theorem, the distribution of X - Y can be approximated by a <u>normal</u> distribution with mean 75 - 57 = 18 and standard deviation 12. Under this approximation, find $\mathbb{P}[X - Y < 0]$, the probability that UConn loses to an Ivy League opponent in a typical matchup.